## Unit 8a: Probability \& Statistics (Compound Events \& Expected Values)

## Probabilistic Reasoning (PR)

G.PR.10: Solve problems involving the probability of compound events to make informed decisions; interpret expected value and measures of variability to analyze probability distributions.

|  <br> Expectations |
| :--- |
| G.PR.10.1 |
| Describe categories <br> of events as subsets <br> of a sample space <br> using unions, <br> intersections, or <br> complements of other | events. Apply the Addition Rule conceptually, $\mathrm{P}(\mathrm{A}$ or $\mathrm{B})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})$ $-\mathrm{P}(\mathrm{A}$ and B$)$, and interpret the answers in context.

## LT \& SC <br> Lesson Activities \& Resources <br> LT: <br> o I am learning to describe categories of events as subsets of a sample space using unions, intersections, or complements of other events.

## SC:

o I can communicate informed decisions by applying the Addition Rule to a problem involving the probability of compound events.
o I can use Venn Diagrams and two-way tables to help visualize events.
o I can use two-way tables to reveal the sample space.
o I can use Venn Diagrams to show intersections of two or more events.

## LA\&R:

o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources.

## How Odd? Instructional Learning Plan

LT:
o I am learning to apply and interpret the general Multiplication Rule conceptually to independent events of a sample space using contingency tables or tree diagrams.

SC:
o I can relate the conditional probability back to the conceptual interpretation of probability studied in previous courses.
o I understand the Multiplication Rule conceptually with limited emphasis on the manipulation of the equation.
o I can use a tree diagram to help me visualize events and probabilities of those events.

|  | LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. <br> The Conditions are Right Instructional Learning Plan |
| :---: | :---: |
| G.PR.10.3 <br> Use conditional probability to interpret risk in terms of decision-making and investigate questions such as those involving false positives or false negatives from screening tests. | LT: <br> o I am learning to use conditional probability to interpret risk in terms of decision-making. <br> o I am learning to investigate questions such as those involving false positives or false negatives from screening tests. <br> SC: <br> o I can answer relevant questions based on the appropriate risk measures. <br> o I can explain how studies and/or models are used to determine risk measures. <br> o I can recognize the chances of a false positive or a false negative is not the same as the chances of having the condition or not having the condition given the test result. <br> o I can interpret and communicate the consequences of making the false positive or false negative errors. <br> o I can interpret the notation for conditional probability in context. <br> LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. |
| G.PR.10.4 <br> Define permutations and combinations and apply this understanding to compute probabilities of compound events and solve meaningful problems. | LT: <br> o I am learning to define permutations and combinations. <br> o I am learning to compute probabilities of compound events using permutations and combinations. <br> o I am learning to solve meaningful problems. <br> SC: <br> o I understand the terms permutation and combination. <br> o I can solve simple problems involving selection and arrangement of objects in a line, including those involving repetition and restriction. <br> o I understand and can apply permutations and combinations. <br> o I can interpret formal notation to communicate about combinations and permutations |


|  | LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. <br> Combinations and Permutations Instructional Learning Plan |
| :---: | :---: |
| G.PR.10.5 <br> Interpret the probability distribution for a given random variable and interpret the expected value. | LT: <br> o I am learning to interpret the probability distribution for a given random variable. <br> o I am learning to interpret the expected value. <br> SC: <br> o I understand that the probabilities in a distribution are between 0 and 1 , and that they should sum to 1 . <br> o I can define a random variable and understand that the sample space consists of all the values the random variable can take. <br> o I can explore and develop an understanding that the expected value is the mean of the probability distribution. <br> o I can solve real-life problems given the expected value and interpret its meaning within context. <br> LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. <br> What Do You Expect? Instructional Learning Plan |
| G.PR.10.6 <br> Develop a probability distribution for variables of interest using theoretical and empirical (observed) probabilities and calculate and interpret the expected value. | LT: <br> o I am learning to develop a probability distribution for variables of interest using theoretical and empirical (observed) probabilities. <br> o I am learning to calculate and interpret the expected value. <br> SC: <br> o I can calculate the probability of all possible outcomes of a given event and display the probability of each graphically. <br> o I understand the sum of all probabilities within one distribution will be 1 ( $100 \%$ ). <br> o I can find the probability of a certain quantity. <br> o I can find the probability of a range of quantities. <br> LA\&R: |


|  | o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. <br> Theoretical and Experimental Probability Instructional Learning Plan |
| :---: | :---: |
| G.PR.10. 7 <br> Calculate the expected value of a random variable and interpret it as the mean of a given probability distribution. | LT: <br> o I am learning to calculate the expected value of a random variable. <br> o I am learning to interpret expected value as the mean of a given probability distribution. <br> SC: <br> o I can use the expected value of a random variable to make informed decisions. <br> o I can calculate the expected value of a random variable as the sum of each $X_{n}{ }^{*} P\left(X_{n}\right)$. <br> o I understand the sum is a weighted average of the outcomes (weighted by the probability). <br> LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. <br> Winning a Lottery Instructional Learning Plan |
| G.PR.10.8 <br> Compare the payoff values associated with the probability distribution for a random variable and make informed decisions based on expected value and measures of variability. | LT: <br> o I am learning to compare the payoff values associated with the probability distribution for a random variable. <br> o I am learning to make informed decisions based on expected value and measures of variability. <br> SC: <br> o I can make decisions about real-life problems considering net value or payoff. <br> o I can understand that two probability distributions can have the same expected value, but one may vary more than the other, and this should be considered in decision-making. <br> o I can compute and interpret expected values for games of chance, insurance policies, and other real-life situations. <br> LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. |


|  | What Do You Expect? |
| :---: | :---: |
| Unit 8b: Categorical Data in two-way frequency tables; conditional probability |  |
| Data \& Statistical Reasoning (DSR); Probabilistic Reasoning (PR) G.DSR.11: Examine real-life situations presented in two-way frequency tables to calculate probabilities, to model categorical data, and to explain real-life phenomena. |  |
| STANDARD \& Expectations | LT \& SC <br> Lesson Activities \& Resources |
| G.DSR.11.1 <br> Construct and summarize categorical data for two categories in two-way frequency tables. | LT: <br> I am learning to construct and summarize categorical data for two categories in two-way frequency tables. <br> SC: <br> o I can identify, calculate, and interpret joint, marginal, and conditional relative frequencies in context of the data. <br> o I can analyze meaningful, real-life data and recognize possible associations and trends in the data. <br> o I can understand and apply concepts of sample space to describe categorical data. <br> LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. <br> More School, Please Instructional Learning Plan |
| G.DSR.11.2 <br> Use categorical data in two-way frequency tables to calculate and interpret probabilities based on the investigation. | LT: <br> o I am learning to use categorical data in two-way frequency tables to calculate and interpret probabilities based on the investigation. <br> SC: <br> o I can use two-way frequency tables to find probabilities for unions and intersections. <br> o I can use two-way frequency tables to compute conditional probabilities <br> LA\&R: <br> o Desmos and 3-Act Tasks; GeoGebra; Quizlet vocabulary \& word wall; See the AP Stat teacher for activities \& resources. |


|  | More School, Please Instructional Learning Plan |
| :--- | :--- |

